



Differentiation Rules Calculus I

General Formulas

1. $\frac{d}{dx} k = 0.$
2. $\frac{d}{dx}(u + v) = \frac{du}{dx} + \frac{dv}{dx}.$
3. $\frac{d}{dx}(u - v) = \frac{du}{dx} - \frac{dv}{dx}.$
4. $\frac{d}{dx}(uv) = u\frac{dv}{dx} + v\frac{du}{dx}.$
5. $\frac{d}{dx}\left(\frac{u}{v}\right) = \frac{v\frac{du}{dx} - u\frac{dv}{dx}}{v^2}.$
6. $y = f(u), u = u(x), \frac{dy}{dx} = \frac{dy}{du} \frac{du}{dx}.$

Basic Functions

1. $\frac{d}{dx} u^n = nu^{n-1} \frac{du}{dx}.$
2. $\frac{d}{dx} \ln |u| = \frac{1}{u} \frac{du}{dx}.$
3. $\frac{d}{dx} e^u = e^u \frac{du}{dx}.$
4. $\frac{d}{dx} \sin u = \cos u \frac{du}{dx}.$
5. $\frac{d}{dx} \cos u = -\sin u \frac{du}{dx}.$
6. $\frac{d}{dx} \tan u = \sec^2 u \frac{du}{dx}.$
7. $\frac{d}{dx} \sec u = \sec u \tan u \frac{du}{dx}.$
8. $\frac{d}{dx} \cot u = -\csc^2 u \frac{du}{dx}.$
9. $\frac{d}{dx} \csc u = -\csc u \cot u \frac{du}{dx}.$
10. $\frac{d}{dx} \ln |\sec u| = \tan u \frac{du}{dx}.$
11. $\frac{d}{dx} \ln |\sec u + \tan u| = \sec u \frac{du}{dx}.$
12. $\frac{d}{dx} \sinh u = \cosh u \frac{du}{dx}.$
13. $\frac{d}{dx} \cosh u = \sinh u \frac{du}{dx}.$
14. $\frac{d}{dx} \tanh u = \operatorname{sech}^2 u \frac{du}{dx}.$
15. $\frac{d}{dx} \sin^{-1} u = \frac{1}{\sqrt{1-u^2}} \frac{du}{dx}.$
16. $\frac{d}{dx} \tan^{-1} u = \frac{1}{1+u^2} \frac{du}{dx}.$
17. $\frac{d}{dx} \sec^{-1} u = \frac{1}{u\sqrt{u^2-1}} \frac{du}{dx}.$
18. $\frac{d}{dx} \sinh^{-1} u = \frac{1}{\sqrt{1+u^2}} \frac{du}{dx}.$
19. $\frac{d}{dx} \tanh^{-1} u = \frac{1}{1-u^2} \frac{du}{dx}.$

Integration Formulas Calculus I

General Formulas

1. $\int k dx = kx + C.$
2. $\int (u + v) dx = \int u dx + \int v dx.$
3. $\int (u - v) dx = \int u dx - \int v dx.$
4. $\int u dv = uv - \int v du.$ (Integration by parts)
5. No "Quotient Rule".
6. $\int f(u) du = \int f(u(x))u'(x) dx.$ (Substitution)

Basic Formulas

1. $\int u^n du = \frac{1}{n+1} u^{n+1} + C; n \neq -1.$
2. $\int \frac{1}{u} du = \ln |u| + C.$
3. $\int e^u du = e^u + C.$
4. $\int \sin u du = -\cos u + C.$
5. $\int \cos u du = \sin u + C.$
6. $\int \sec^2 u du = \tan u + C.$
7. $\int \sec u \tan u du = \sec u + C.$
8. $\int \csc^2 u du = -\cot u + C.$
9. $\int \csc u \cot u du = -\csc u + C.$
10. $\int \tan u du = \ln |\sec u| + C.$
11. $\int \sec u du = \ln |\sec u + \tan u| + C.$
12. $\int \sinh u du = \cosh u + C.$
13. $\int \cosh u du = \sinh u + C.$
14. $\int \operatorname{sech}^2 u du = \tanh u + C.$
15. $\int \frac{1}{\sqrt{a^2-u^2}} du = \sin^{-1} \frac{u}{a} + C.$
16. $\int \frac{1}{a^2+u^2} du = \frac{1}{a} \tan^{-1} \frac{u}{a} + C.$
17. $\int \frac{1}{u\sqrt{u^2-a^2}} du = \frac{1}{a} \sec^{-1} \frac{u}{a} + C.$
18. $\int \frac{1}{\sqrt{a^2+u^2}} du = \sinh^{-1} \frac{u}{a} + C.$
19. $\int \frac{1}{a^2-u^2} du = \frac{1}{a} \tanh^{-1} \frac{u}{a} + C.$